

Objective Questions (Real no system and sequences)

Q.1. A subset of Real numbers is said to be bounded if it is

- (a) Bounded above (b) Bounded below
(c) Bounded below and bounded above (d) None of these

Q.2. If the supremum and infimum for a set are same then the set is

- (a) Empty (b) can't be possible
(c) singleton (d) None of these

Q.3. The open interval (a, b) is a h.d. of

- (a) a (b) b (c) both a and b
(d) each of its points

Q.4. The set of isolated points is called

- (a) open set (b) derived set
(c) discrete set (d) None of these

Q.5. If $\bar{A} = A$ then A is

- (a) open set (b) perfect set
(c) closed set (d) discrete set

Q.6. The set of all irrational numbers is

- (a) finite (b) uncountable
(c) countable (d) None of these

Q.7. If $x, y, z \in \mathbb{R}$, the set of real numbers then which one of the following relation does not hold good.

- (a) $x, y > 0 \Rightarrow x - y > 0$ (b) $x, y > 0 \Rightarrow x + y > 0$
(c) $x, y > 0 \Rightarrow x \cdot y > 0$ (d) None of these

Q.8. If S is subset of real numbers which is bounded below the $\inf(S)$ is

- (a) prime number (b) a point closure to S
(c) not a point closure to S (d) None of these

Q.9. The empty set \emptyset is

- (a) open set (b) closed set
(c) both open and closed set (d) None of these

Q.10. The intersection of all sets of the form $(-\frac{1}{n}, \frac{1}{n})$ $n \in \mathbb{N}$ is

- (a) an open set (b) not an open set
(c) singleton (d) none of these

Q.11. Let $A = [9, 6]$ then

(a) $\sup(A) \in A$ (b) $\inf(A) \in A$

(c) both $\sup(A) \notin A$ & $\inf(A) \notin A$ (d) $\sup(A) \notin A$

Q.12. Let $S = \left\{ 1 + \frac{(-1)^n}{n} \mid n \in \mathbb{N} \right\}$ then \sup & \inf of S are

(a) $(0, 1)$ (b) $(1, 3/2)$ (c) $(0, 3/2)$ (d) $(-1, 0)$

Q.13. The domain of the sequence is always

(a) real numbers (b) natural numbers
(c) integers (d) none of these

Q.14. A sequence is said to be bounded if for any $k > 0$

(a) $k < s_n < k + \epsilon \forall n \in \mathbb{N}$ (b) $s_n > k \forall n \in \mathbb{N}$
(c) $k < s_n < k + \epsilon \forall n \in \mathbb{N}$ (d) none of these

Q.15. If $\langle s_n \rangle$ diverges to ∞ and $\langle t_n \rangle$ is bounded

then $\langle s_n + t_n \rangle$

(a) Converges (b) diverges to ∞
(c) is bounded (d) none of these

Q.16. Every bounded sequence has at least

(a) one limit point (b) two limit points
(c) no limit point (d) none of these

Q.17. If $\lim s_n = l_1$ and $\lim t_n = l_2$ then

$\lim_{n \rightarrow \infty} \frac{s_n + t_n + s_n t_n}{s_n t_n}$ is equal to

(a) l_1 (b) l_2 (c) $l_1 l_2$ (d) None of these

Q.18. Every Cauchy sequence is

(a) convergent (b) bounded
(c) both (a) & (b) (d) None of these

Q.19. which is not True

(a) every convergent sequence is bounded
(b) every bounded sequence is convergent
(c) the sequence $\langle (-1)^n \rangle$ is not convergent
(d) the sequence $\langle 1/n \rangle$ converges to zero

Q.20. which of the following is a bounded sequence

(a) $\langle (-1)^n, \frac{n}{n+1} \rangle$ (b) $\langle 2, 3, 5, 7, 11, \dots \rangle$
(c) $\langle (-1)^n, n \rangle$ (d) none of these