

Ex. 1, B-126 Algebra & Trigonometry

Topic - Trigonometry

Q.1 Find the value of $A \neq B$, if $A + iB = \frac{3-2i}{7+4i}$

Q.2 Show that $\sinh(x+y) \cosh(x-y) = \frac{1}{2} (\sinh 2x + \sinh 2y)$.

Q.3. Resolve $\sin^2(x+iy)$ in to real and imaginary parts.

Q.4. If $\tan(\theta + i\phi) = \tan \alpha + i \sec \alpha$, then prove that

$$e^{2\phi} = \frac{1}{2} \cot \frac{1}{2} \alpha \text{ and } 2\theta = n\pi + \frac{\pi}{2} + \alpha$$

Q.5. If $A + iB = C \tan(x+iy)$, then prove that

$$\tan 2x = \frac{2CA}{C^2 - A^2 - B^2}$$

Q.6 Prove that $\log \tan\left(\frac{\pi}{4} + i \frac{\alpha}{2}\right) = i \tan^{-1}(\sinh \alpha)$

Q.7 Show that $\tan\left(i \log \frac{a-ib}{a+ib}\right) = \frac{2ab}{a^2 - b^2}$

Q.8 Prove that ~~$i = e^{i\pi/2}$~~ $i = e^{-i(4n+1)\pi/2}$

Q.9. If $(a+ib)^n = m^{k+iy}$, then prove that

$$\frac{y}{x} = \frac{2 \tan^{-1}(b/a)}{\log(a^2 + b^2)}$$

Q.10 Prove that $\frac{\pi}{8} = \frac{1}{1.3} + \frac{1}{5.7} + \frac{1}{9.11} + \dots$ a.d.u.f.

Q.11 Show that $\left[\frac{1}{2} + \frac{1}{5} + \frac{1}{8}\right] - \frac{1}{3} \left[\frac{1}{2^3} + \frac{1}{5^3} + \frac{1}{8^3}\right] + \frac{1}{5} \left[\frac{1}{2^5} + \frac{1}{5^5} + \frac{1}{8^5}\right] - \dots = \frac{1}{2}$

Q.12 Sum the series $1 + e^{\cos \alpha} \cos(\sin \alpha) + \frac{1}{2!} e^{2 \cos \alpha} \cos(2 \sin \alpha) + \dots$ a.d.u.f.

Q.13 Sum the series $\cos \alpha - \frac{\cos(2+2B)}{3!} + \frac{\cos(2+4B)}{5!} + \dots$ a.d.u.f.

Q.14 Sum the series $\tan^{-1}\left(\frac{1}{1+1+2}\right) + \tan^{-1}\left(\frac{1}{1+2+2^2}\right) + \tan^{-1}\left(\frac{1}{1+3+3^2}\right) + \dots$ a.d.u.f.

Q.15. Find the sum of the series

$$\sin \alpha - \frac{\sin 3\alpha}{2!} + \frac{\sin 5\alpha}{4!} + \dots$$

Q.16 state and prove Gregory's series.

Q.17 Sum the series.

$$1 + e \cosh \theta + e^2 \cosh 2\theta + e^3 \cosh 3\theta + \dots$$